

## Reduction of the uncertainties in the water level-discharge relation of a 1D hydraulic model in the context of operational flood forecasting

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Johan Habert, Sophie Ricci, Olivier Thual, Etienne Le Pape, Andrea Piacentini, et al.. Reduction of the uncertainties in the water level-discharge relation of a 1D hydraulic model in the context of operational flood forecasting. Journal of Hydrology, Elsevier, 2016, <10.1016/j.jhydrol.2015.11.023>. <hal-01244241>

# HAL Id: hal-01244241 https://hal.archives-ouvertes.fr/hal-01244241

Submitted on 23 Dec 2015

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#### Elsevier Editorial System(tm) for Journal of Hydrology Manuscript Draft

Manuscript Number:

Title: Reduction of the uncertainties in the water level-discharge relation of a 1D hydraulic model in the context of operational flood forecasting.

Article Type: Review Article

Keywords: Hydraulic modeling Flood forecasting Data assimilation Uncertainty reduction

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## Reduction of the uncertainties in the water level-discharge relation of a 1D hydraulic model in the context of operational flood forecasting

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#### Abstract

This paper presents a data-driven hydrodynamic simulator based on the 1-D hydraulic 1 solver dedicated to flood forecasting with lead time of an hour up to 24 hours. The goal of 2 the study is to reduce uncertainties in the hydraulic model and thus provide more reliable 3 simulation and forecast in real time for operational use by the national hydrometeorological flood forecasting center in France. Previous studies have shown that sequential assimilation 5 of water level or discharge data allows to adjust the inflows to the hydraulic network resulting 6 in a significant improvement of the discharge while leaving the water level state imperfect. 7 Two strategies are proposed here to improve the water level-discharge relation in the model. 8 At first, a modeling strategy consists in improving the description of the river bed geometry 9 using topographic and bathymetric measurements. Secondly, an inverse modeling strategy 10 proposes to locally correct friction coefficients in the river bed and the flood plain through 11 the assimilation of in-situ water level measurements. This approach is based on an Extended 12 Kalman filter algorithm that sequentially assimilates data to infer the upstream and lateral 13 inflows at first and then the friction coefficients. It provides a time varying correction of the 14 hydrological boundary conditions and hydraulic parameters. 15

The merits of both strategies are demonstrated on the Marne catchment in France for eight validation flood events and the January 2004 flood event is used as an illustrative example throughout the paper. The Nash-Sutcliffe criterion for water level is improved from

0.135 to 0.832 for a 12-hour forecast lead time with the data assimilation strategy. These 19 developments have been implemented at the SAMA SPC (local flood forecasting service in 20 the Haute-Marne French department) and used for operational forecast since 2013. They 21 were shown to provide an efficient tool for evaluating flood risk and to improve the flood 22 early warning system. Complementary with the deterministic forecast of the hydraulic state, 23 an estimation of an uncertainty range is given relying on off-line and on-line diagnosis. The 24 possibilities to further extend the control vector while limiting the computational cost and 25 equifinality problem are finally discussed. 26 Keywords:

Hydraulic modeling, Flood forecasting, Data assimilation, Uncertainty reduction

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#### 27 1. Introduction

Flooding causes important social, environmental and economic losses and is likely to be 28 aggravated by climate change over the next decades. For example, flooding of the Var river 29 in the South-East of France in 2010 resulted in a 700 million euros loss and 25 victims (22). 30 Worldwide, national or international operational flood forecasting centers are in charge of 31 providing water level predictions and flood risks at short- to medium-range lead time (from 32 several hours to a few days) that are of great importance for civil protection. To this end, op-33 erational centers aim at providing an accurate forecast of the hydraulic variables (i.e., water 34 level and discharge) along the monitored network. This forecast relies on the complemen-35 tary use of numerical models and observations (18). For instance, the UK Environment 36 Agency in collaboration with the Met Office has developed the National Flood Forecast-37 ing System (NFFS) in order to access to real-time forecasts from a large set of hydrologic 38 modeling tools (38; 37). In the Philippines, the Metro Manila model is used operationally 39 to issue 24-hour lead time forecasts using precipitation and water level measurements that 40 are collected and transmitted in real time (20). In France, since 2006, the national and hy-41 drometeorological flood forecasting center (SCHAPI – Service Central d'Hydrométéorologie 42 et d'Appui à la Prévision des Inondations), in collaboration with the 22 local flood forecast-43 ing services (SPC – Service de Prévision des Crues), produces a twice-daily vigilance map 44 available for governmental authorities and general public (http://www.vigicrues.gouv.fr). 45 Meteorological, hydrologic and geographic data (bathymetry, topography), are used as in-46 puts to hydraulic models that are integrated in forecast mode to describe water level and 47 discharge at a limited number of observing stations over 22,000 km of rivers in France. These 48 hydraulic variables are then translated into a colored flood risk map available online. On 49 a larger scale, the European Flood Awareness System (EFAS) as part of the Copernicus 50 Emergency Management System provides probabilistic flood alert information more than 48 51 hours in advance to national authorities. This alert system covers the main European rivers 52 on a 5-km grid using a distributed hydrologic rainfall-runoff-routing model (LISFLOOD) as 53 well as ensemble weather forecasts and real-time weather observations (8; 34). 54

The capacity for real-time anticipation of extreme flood events remains limited due to 55 several sources of uncertainty in hydraulic models. On the one hand, forcing data that 56 represent boundary conditions for hydraulic models usually result from the transformation 57 of uncertain observed water levels into discharges with an uncertain rating curve (7; 3), or 58 from discharges forecasted by uncertain hydrologic models. Another source of uncertainty is 59 the description of the river channel and flood plain geometry. This requires on-site measure-60 ments of topographic and bathymetric profiles to provide a spatially-distributed geometry. 61 On the other hand, the equations that are solved by models are based on simplification and 62 parametrization of the physics. The parametrization schemes are calibrated to adjust the 63 model behavior to observed water levels, typically, through the calibration of friction coeffi-64 cients. The calibration of the river bed and flood plain friction coefficients is usually achieved 65 once for all using a batch of observations such as water level from a limited number of flood 66 events, thus providing time-invariant values for the model parameters. It is important to 67 mention that errors in the model inputs and in the model equations are sometimes diffi-68 cult to discriminate (35; 30). These uncertainties usually translate into errors in the model 69 representation of the water level-discharge (H-Q) relation that is not coherent with that 70 from the reality. In practice, this inconsistency can be reduced when complementary data 71 become available to improve the model, for instance LIDAR data for bathymetry (horizontal 72 resolution of one point per square meter; 10 to 30 cm of vertical accuracy). When no ad-73 ditional data are available to improve the model geometry, the error between the simulated 74 and the observed hydraulic states must be accounted for by adjusting the model parameters 75 and/or the model state itself. Many studies have attempted to account for uncertainties 76 at varying levels (36; 19), for instance by analyzing the uncertainty in hydrologic predic-77 tion based on the Generalized Likelihood Uncertainty Estimation (GLUE) (5; 2; 25; 33), 78 Markov chain Monte Carlo (MCMC) (16), Bayesian inference (27) and Data Assimilation 79 (DA) (19; 24; 10; 9). 80

<sup>81</sup> DA offers a convenient and cost-effective framework, compared to MCMC and Bayesian <sup>82</sup> inference, to overcome some limits of the classical calibration process for model parame-<sup>83</sup> ters: observations and simulation outputs are combined along with their respective errors to

estimate an optimal set of model parameters and thereby reduce simulation uncertainties. 84 Furthermore, as the DA algorithm is sequentially applied, the analysis allows for a temporal 85 variation of model parameters errors. The classical approach in DA for meteorology and 86 oceanography is to directly correct the model output variables (also called state estimation). 87 In the hydrology and hydraulic literature, the estimation of uncertainty in model parame-88 ters has been extensively investigated in addition to the more traditional state estimation 89 approach. Sequential state estimation for hydraulic applications was indeed found to have 90 limited impact on the forecast performance due to the limited persistence of the model a 91 initial condition. In contrast, the forecast lead time can be significantly improved via the 92 correction of the hydrologic forcing (14; 1; 31) or of the model parameters (11). Through 93 the inclusion of parameters in the DA process, it is assumed that the forecast uncertainty 94 can be efficiently reduced over a time window for which the errors statistics in the model 95 parameters are stationary. State and parameter correction can be performed independently, 96 or simultaneously (24; 23) with an augmented state as illustrated in (15). For example, (26)97 focused on state estimation and assimilated water level observation derived from spaceborne 98 imaging and digital terrain model to estimate discharge in an un-gauged basin simulated 99 by a coupled hydrologic and hydrodynamic model. (14) and (21) used ensemble-based ap-100 proaches (the Ensemble Kalman Filter – EnKF – and particle filters, respectively) to update 101 the state but also to infer the upstream boundary conditions. (4) explored the assimilation 102 of hydrologic data into operational hydrologic forecast to correct several input parameters 103 including river bed friction coefficients. 104

The present study illustrates how errors in the water level-discharge relation of a 1D hy-105 draulic model can be accounted for in the context of operational flood forecasting following 106 two different approaches. The first method is based on the assumption that additional data 107 on the river bed geometry are available to directly improve the model H - Q relation. In 108 the following, this approach is referred to as experiment BATHY. For the second method, 109 it is assumed that the only additional data available are in-situ water level measurements, 110 which are used in real time to adjust the river bed and flood plain friction coefficients in the 111 model using a DA algorithm. In the following, this approach is referred to as experiment 112

ASSIM. A time-dependent correction of the friction coefficients is provided by DA in order 113 to account for errors in the friction and bathymetry description that vary along with the 114 flow as water level reaches different portions of the described geometry. It should be noted 115 that the errors in the model H - Q relation are potentially larger at high flow since the 116 flood plain topography is not well known and since the model is not well calibrated. Thus, 117 this study aims at demonstrating that both approaches BATHY and ASSIM can signifi-118 cantly improve the model H - Q relation and subsequently the simulated hydraulic state. 119 This work is carried out in the context of operational flood forecasting at the SAMA (Seine 120 Amont Marne Amont) SPC for the Marne catchment in France. SAMA uses the 1D hy-12: draulic model MASCARET (12) developed by LNHE (Laboratoire National d'Hydraulique 122 et d'Environnement) from EDF-R&D (Electricité De France – Recherche et Développement) 123 to simulate real-time discharge or water level forecasts at six observing stations on the up-124 stream part of the Marne river. Maximum forecast lead time for each site is between 5 and 125 21 hours according to the transfer time along the hydraulic network. The reference model 126 for this work, referred to as experiment REF in the following, results from a classical batch 127 calibration procedure of the un-gauged upstream and lateral inflows to the model as well 128 as of the river bed and flood plain friction coefficients. In this context, (31) demonstrated 129 that the assimilation, based on an Extended Kalman Filter (EKF) algorithm, of water level 130 observations to correct hydrologic boundary conditions and hydraulic model parameters on 131 the Adour catchment with MASCARET improves flood forecasting by 60 % for 1-hour lead 132 time and by 25 % for 12-hour lead time. A similar approach using discharge data was then 133 applied to the Marne catchment to specify upstream and lateral inflows (13), resulting in 134 the significant improvement of the simulated discharge state, while the simulated water level 135 state remained imperfect. The correction of un-gauged lateral and upstream inflows with 136 DA offers an alternative solution to the classical batch calibration procedure by considering 137 a time-varying estimation of the boundary conditions. In the present work, this corresponds 138 to the first step of the DA method referred to as experiment ASSIM1 in the following. Fur-139 ther improvement on the river bed and flood plain friction coefficients in the neighborhood of 140 the observing stations is obtained with water level assimilation. This represents the second 141

step of the DA method referred to as experiment ASSIM2 in the following. The method ASSIM is therefore a two-step DA procedure: ASSIM1 allows for the correction of upstream and lateral inflows and ASSIM2 allows for the correction of river bed and flood plain friction coefficients. The sequential application of both steps in ASSIM is referred to as experiment ASSIM1+ASSIM2.

The structure of the paper is as follows: Section 2 provides a description of the Marne 147 catchment and of the materials (hydraulic model, DA method) used to perform flood fore-148 casting. The evaluation of the linearity of the water level with respect to the friction coeffi-149 cients is investigated. The limitations of the reference model REF are highlighted and the 150 two-step DA strategy ASSIM is presented in detail. In Sect. 3, the results of both BATHY 15: and ASSIM approaches are presented using the January 2004 flood event as an illustrative 152 example. The operational implementation of the ASSIM approach at the SAMA SPC is 153 described in Sect. 4. Conclusions and perspectives for this work are given in Sect. 5. 154

#### <sup>155</sup> 2. Materials and methods

#### 156 2.1. The 1D hydraulic model MASCARET

The Marne river is an important tributary of the Seine river in France. Its source is 157 located on the Langres plateau in the Haute-Marne department. A mono-dimensional hy-158 draulic model is used to simulate the hydrodynamics of the 180-km Marne river as presented 159 in Figure 1. This study is carried out in the upstream part of the Marne river where flash 160 floods frequently occur; for instance, in December 2011, the discharge at Condes raised 161 from 25 to 125  $m^3/s$  in 24 hours. Upstream boundary conditions (black dots in Figure 1) 162 for the hydraulic network are described with observed water levels that are translated into 163 discharges with a local rating curve; the downstream boundary condition at Chamouilley 164 is also described with a local rating curve. There are six observing stations located on 165 the main stream of the river (black triangles in Figure 1) where water level is measured 166 hourly. These data are provided by the DREAL (Direction Régionale de l'Environnement, 167 de l'Aménagement et du Logement) hydrometeorological service in the Champagne-Ardenne 168 region. 169

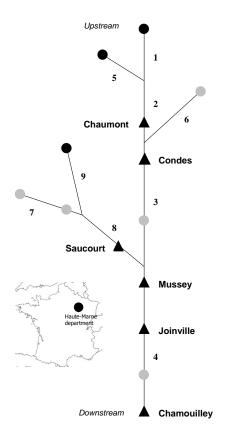


Figure 1: Schematic of the Marne model hydraulic network (Haute-Marne, France). Observed upstream flows are represented with black dots; additional inflows are represented with grey dots; and observing stations over the hydraulic network are represented with triangles.

Along this hydraulic network, the 1D form of the Saint-Venant equations is solved with the MASCARET (12) software developed by EDF-R&D and CEREMA (Centre d'Etudes et d'Expertise sur les Risques, l'Environnement, la Mobilité et l'Aménagement), widely used for modeling flood events, submersion waves resulting from the failure of hydraulic infrastructures, river control, and channel waves propagation. The 1D Saint-Venant equations read (non-conservative form):

$$\frac{\partial S}{\partial t} + \frac{\partial Q}{\partial x} = q_a \quad , \ \frac{\partial Q}{\partial t} + \frac{\partial QV}{\partial x} + gS(\frac{\partial Z}{\partial x} + J + J_s) = 0 \ with \ J = \frac{Q^2}{S^2 K_s^2 R_H^{4/3}}.$$
(1)

where S [m<sup>2</sup>] is the river section, Q [m<sup>3</sup>/s] is the discharge,  $q_a({
m x},t)$  is the lateral lineic

discharge,  $K_s$  [m<sup>1/3</sup>.s<sup>-1</sup>] is the friction coefficient,  $R_H$  is the hydraulic radius, g is the gravity, J and  $J_s$  represents regular and singular head losses respectively. The river section S is, for each location x, a function of the water level  $H = Z(x,t) - Z_{bottom}(x,t)$ , where Z(x,t) [m] is the free surface height and where  $Z_{bottom}$  [m] corresponds to the river bed bathymetry. The unsteady kernel of MASCARET was used in this study.

The Marne terrain model was built with 110 topographic and bathymetric cross sections; 182 it was calibrated in 2011 using a batch of water level and discharge measurements from ten 183 flood events at Chaumont, Condes, Saucourt, Mussey, Joinville and Chamouilley. The 184 model was then validated over eight independent flood events that occurred between 2004 185 and 2013; these events can be classified in three types: two events with a maximum discharge 186 of  $100 \text{ m}^3/\text{s}$  at Mussey, two events with a maximum discharge at Mussey ranging between 187 115 and 240  $m^3/s$ , and three stronger events with a maximum discharge at Mussey above 188  $260 \text{ m}^3/\text{s}$  (among which the January 2004 flood event used in this paper for illustrative 189 purposes). Five upstream and lateral inflows (grey dots in Figure 1) were added to the 190 model to represent additional water input to the network. At these five locations, despite 191 the lack of hydrologic rainfall-runoff model, the hydrograph is described as proportional to 192 a mean upstream area hydrograph; the multiplicative coefficients used for the model in the 193 present work were optimized by a batch calibration procedure. Additionally, the river bed 194 and flood plain friction coefficients (denoted respectively by m and n) were calibrated by 195 minimizing simulated and observed discharge differences; the resulting calibrated friction 196 coefficients that have a straightforward influence on the H - Q relation in the model are 197 given in Table 1. In the following, the model with batch calibration corresponds to the 198 reference model denoted by REF. 199

The Nash-Sutcliffe criteria for water level  $N_H$  and discharge  $N_Q$  were calculated for the eight validation flood events for each observing station using the following formulation given 202 for Q:

$$N = 1 - \frac{\sum_{i=1}^{n} (Q_i^{obs} - Q_i^{sim})^2}{\sum_{i=1}^{n} (Q_i^{obs} - \overline{Q}^{obs})^2},$$
(2)

where  $Q_i^{obs}$  and  $Q_i^{sim}$  correspond to the observed and simulated discharges at time indexed 203 by *i*, and where  $\overline{Q}^{obs}$  denotes the time-averaged value of the observed discharges. The 204 Nash-Sutcliffe criteria results are presented in Table 1. In general, the quality of the results 205 decreases from upstream to downstream as the use of mean multiplicative coefficients gener-206 ates errors in the lateral and upstream inflows estimation. Additionally, the Nash-Sutcliffe 207 criteria computed with respect to discharge Q are generally better than when computed 208 with respect to water level H, especially at Mussey (Reach 4, Portion 1 in Table 1). It 209 should be noted that there is no rating curve available at Joinville, thus no discharge data 210 at this observing station. For the January 2004 flood event used in this work for illustra-211 tive purposes, the Nash-Sutcliffe criteria associated with the REF model and presented in 212 Table 2 are respectively 0.773 and 0.894 for water level and discharge. The criteria are here 213 computed in re-analysis mode that corresponds to a 0-h forecast lead time (details are given 214 in Sect. 2.2). REF (dashed lines) and observed (dotted lines) hydraulic states at Mussey 215 are compared in Figure 2 over the January 2004 flood event (thin lines correspond to water 216 level, thick lines correspond to discharges). The difference between REF and observations 217 varies over time for both water level and discharge, thus arguing for a time-dependent cor-218 rection as enabled by DA in Sect. 2.2. It is important to notice that the sign of the error 219 in discharge and in water level are different for high flow conditions (flood peak from day 4 220 to day 5), while similar away from the flood peak. For high water levels, the discharge is 221 slightly overestimated (by  $25 \text{ m}^3/\text{s}$  at day 5), whereas the water level is significantly un-222 derestimated (by 0.4 m at day 5). During this period, the H - Q relation in the model is 223 incorrect, a negative correction in the discharge would further deteriorate the water level 224 state. Thus, for this event, the batch calibration process is to fail at providing parameters 225 (friction coefficients and upstream/lateral inflows) that would improve both discharge and 226

Reaches	Portions	Length	m	n	Observing stations	$N_H$	$N_Q$
1	1	5,172	24	14			
2	1	21,753	24	14	Chaumont	0.922	
3	1	660	36	22	Condes	0.821	0.835
9	2	44,842	24	14			
	1	578	20	13	Mussey	0.544	0.743
4	2	8,200	24	18			
	3	300	14	8	Joinville	0.531	
	4	26,383	24	14	Chamouilley	0.614	0.621
5	1	$4,\!150$	24	14			
6	1	27,101	24	14			
7	1	7,600	9	7			
	1	16,266	9	7			
8	2	500	13	8	Saucourt	0.797	0.821
	3	$5,\!680$	9	7			
9	1	10,819	9	7			

water level at the flood peak (the same assumption seems legitimate at Joinville). It is then obvious that the reference model (REF) should be improved as explained in the following.

Table 1: Mean friction coefficients obtained after calibration for the river bed (m) and the flood plain (n) in  $[m^{1/3}.s^{-1}]$ , as well as Nash criteria for water level  $(N_H)$  and discharge  $(N_Q)$  calculated for eight validation flood events and for reaches 1 to 9 over the Marne model hydraulic network. Reaches lenghts are in meters.

#### 229 2.2. Sequential DA method

230 2.2.1. DA algorithm

The DA method (ASSIM) is a two-step procedure using an EKF algorithm.

The first step ASSIM1 consists in correcting the upstream and lateral inflows to the model using discharge data, with the objective to improve the simulated discharge. The

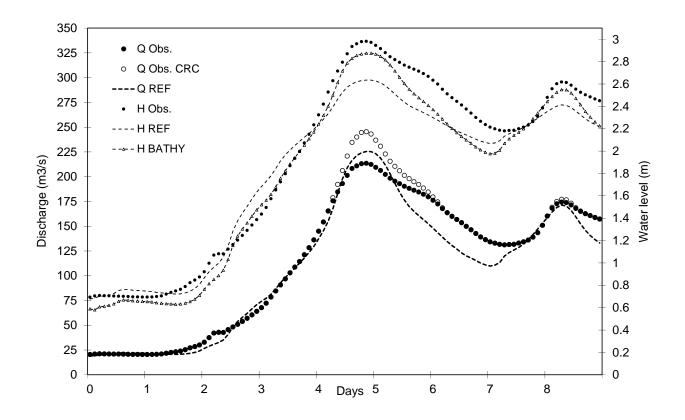


Figure 2: Simulated water levels (thin lines) and discharges (thick lines) at Mussey for REF (dashed line) and BATHY (dashed line with triangle – discharges are unchanged) for the January 2004 flood event. Observations are represented with small and large black dots for water level and discharge, respectively. Circles represent the discharge observations obtained with the Corrected Rating Curve (CRC).

ASSIM1 method is presented in details in (31) and (13). For the Marne applicative test case, discharge observations (Condes, Mussey, Chamouilley and Saucourt) are assimilated to correct the five upstream and lateral inflows along the hydraulic network (represented by grey dots in Figure 1) in order to correctly represent discharge.

In spite of the discharge improvement, when the model H - Q relation is incorrect (at high flow), the simulated water level remains imperfect. These errors are here accounted for in the second step ASSIM2, which uses water level data to locally correct river bed and flood plain friction coefficients in the neighborhood of the observing stations. The batch calibration process leads to an estimate that allows, on average, the model to correctly

	$N_H$	$N_Q$
REF	0.773	0.894
BATHY	0.923	0.897
ASSIM1	0.784	0.976
BATHY+ASSIM1	0.986	0.987
ASSIM1+ASSIM2	0.97	0.978

Table 2: Nash-Sutcliffe criteria for REF, BATHY, ASSIM1 and ASSIM1+ASSIM2 experiments for water level  $(N_H)$  and discharge  $(N_Q)$  in re-analysis mode for the January 2004 flood event at Mussey.

simulate a set of flood events. Depending on the choice of this set of events, the calibrated 243 friction coefficients might be better fitted for low, medium or high flow. Usually, high flow 244 are not well represented. It thus makes sense to look for a time-varying correction of the 245 friction coefficients during a flood event. Additionnaly, the bathymetry is described from a 246 limited number of measured cross sections. The correction of the friction coefficients offers 247 a way to also account for the uncertainty related to bathymetry. In the present study, the 248 friction coefficients are corrected over a 600-m section in the vicinity of the observing station 249 at Mussey (Portion 1 of reach 4) and over a 300-m section in the vicinity of Joinville (Portion 250 3 of reach 4). These coefficients were chosen as their uncertainty has a significant influence 25 on the simulated water level at the observing stations; still the following method could be 252 applied to any friction coefficient for the hydraulic network. The friction coefficients in the 253 river bed and in the flood plains, respectively denoted by m and n, are gathered in the 254 control vector  $\mathbf{x}$  of size s = 4 in the present case study. The background values in  $\mathbf{x}^b$  are 255 those specified from the calibration procedure ( $m^b = 20$  and  $n^b = 13$  for Mussey;  $m^b = 14$ 256 and  $n^b = 8$  for Joinville). The errors in m and n are supposed to be uncorrelated, and the 257 respective standard deviation (STD) are set according to the variability in the calibration 258 procedure ( $\sigma_m^b = 3$  and  $\sigma_n^b = 4$  at Mussey;  $\sigma_m^b = 3$  and  $\sigma_n^b = 2$  at Joinville). Hourly water 259 level observations are assimilated over a time window at Mussey and Joinville and gathered 260 in the observation vector  $\mathbf{y}^o$  of size p. The errors in the water level observations are supposed 261

to be uncorrelated; the observation error STD  $\sigma_o$  is set to 0.025 m to account for errors in the adjustment of the measurement pressure tube.

Following the classical equations of the Kalman filter (17), the analysis vector  $\mathbf{x}_k^a$  for cycle k can be formulated as a correction to the background vector  $\mathbf{x}_k^b$  as follows:

$$\mathbf{x}_{k}^{a} = \mathbf{x}_{k}^{b} + \mathbf{K}_{k} \Big( \mathbf{y}_{k}^{o} - H_{k}(\mathbf{x}_{k}^{b}) \Big), \tag{3}$$

where  $\mathbf{K}_{k} = \mathbf{B}_{k}\mathbf{H}_{k}^{T}(\mathbf{H}_{k}\mathbf{B}_{k}\mathbf{H}_{k}^{T} + \mathbf{R}_{k})^{-1}$  is the gain matrix,  $\mathbf{B}_{k}$  and  $\mathbf{R}_{k}$  are respectively the background and observation errors covariance matrices, and  $\mathbf{H}_{k}$  is the Jacobian of  $H_{k}$  at  $\mathbf{x}_{k}^{b}$ . The analysis error covariance matrice is:

$$\mathbf{A}_{k} = (\mathbf{I} - \mathbf{K}_{k} \mathbf{H}_{k}) \mathbf{B}_{k}.$$
(4)

The generalized observation operator  $H_k$  is used to describe the model counterpart of the 269 observations  $\mathbf{y}_k^o = H_k(\mathbf{x}_k)$  associated with the control vector  $\mathbf{x}_k$ . It consists in, first integrat-270 ing the hydraulic model using the friction coefficients in  $\mathbf{x}^b$ , then selecting the corresponding 271 simulated water level at the observed point and time. This operator is non-linear with re-272 spect to  $\mathbf{x}$  as it implies the integration of the hydraulic model; this issue will be further 273 investigated in Sect. 2.2.2 as it is a limiting point for the EKF algorithm optimality. The 274 Jacobian  $\mathbf{H}_k$  of the observation operator  $H_k$  is a  $s \times p$  matrix: each column represents the 275 variation in the hydraulic variables at the observing locations and times that are due to the 276 perturbation of an element of the control vector (corresponding to one friction coefficient 277 over a given location). In the present work, it is conveniently computed in the vicinity of 278 the background vector at the analysis time k with a finite difference scheme that requires 279 additional hydraulic model integrations; these independent integrations are run in parallel 280 using the Parasol functionality of the OpenPALM dynamic coupler (6), a framework that 281 is convenient to develop DA methods in a modular way. The Jacobian matrix is computed 282 for each analysis cycle as the impact of a perturbation in the friction coefficients on the 283 hydraulic variables depends on the hydraulic state itself. 284

Since there is no explicit propagation model for parameters (29; 24; 28; 32), the usual propagation steps of the KF algorithm are irrelevant here; a persistence model is often

assumed for the parameters between the analysis cycles. In the present implementation, the 287 background vector  $\mathbf{x}_k^b$  and the background error covariance matrix  $\mathbf{B}_k$  are kept invariant 288 between the cycles (for every cycle k). For that reason, the present EKF algorithm can 289 be considered as an invariant EKF (relatively to the background information). It is worth 290 noting that for a given cycle, the initial condition for the background simulation is derived 291 from the analysis simulation obtained during the previous cycle; consequently, each cycle 292 restarts with an improved initial condition. Thus, the background 78-hour run differs from 293 the corresponding portion (in time) of the continuous reference run (REF) since both runs 294 start from a different model state at the cycle initial time. It is also worth mentioning that 295 advanced pseudo-model for parameters could be implemented; this question will be addressed 296 in further work. The small size of the control vector (less than 10 for the Marne test case) 297 enables the use of an EKF algorithm, involving matrix operations for the computation of 298 the gain matrix along with a finite difference scheme for the computation of the generalized 299 observation operator Jacobian. 300

The cycling of the analysis is presented in Figure 3 for ASSIM1 and in Figure 4 for 301 ASSIM2 following ASSIM1. The assimilation is performed over a cycle k of 66 hours with 302 54 hours of re-analysis and 12 hours of forecast at Mussey. The forecast period is adjusted for 303 each observing station and decreases going downstream. Over the 54-hour re-analysis period, 304 the hydrologic upstream and lateral forcings are supposed to be known (either observed or 305 calibrated). Over the forecast period, the forcings are supposed to be unknown and set 306 constant to the last known value. The 54-hour re-analysis period corresponds to a 48-hour 307 period over which the model adjusts to the initial state, plus a 6-hour period over which 308 observations are assimilated using the EKF algorithm. Hence, the size of the observation 309 vector in the present study is p = 12. The last observation time from which the forecast 310 integration starts is the analysis time T. For cycle k, in ASSIM1 (Figure 3), over the 6-hour 311 assimilation period (hatching area), the background issued from the previous analysis cycle 312 (solid line) and observed discharges (black dots) are compared and a correction to the inflows 313 is obtained through the EKF analysis step. The correction is applied over the re-analysis 314 and the forecast periods, thus assuming that the nature of the errors in the upstream and 315

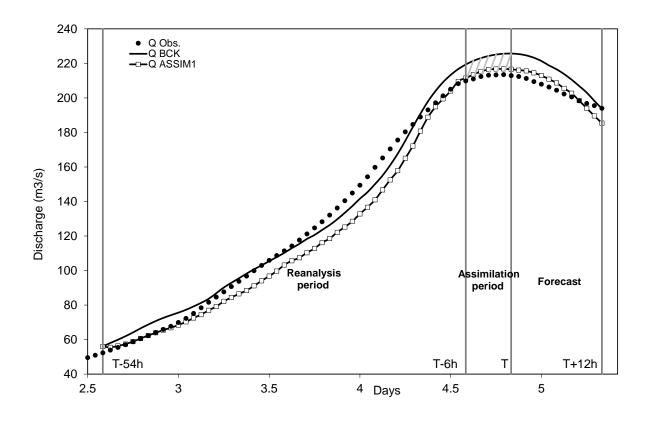


Figure 3: Observed (black dots), background from previous cycle (BCK solid line) and analyzed discharges (squared solid line) for the ASSIM1 approach at the flood peak at Mussey for the January 2004 flood event for T = 417,600 s = 4.83 days.

lateral inflows remains the same over the forecast period. The analyzed forcings are used to achieve a new model integration (over the 66-hour time period), which provides a better discharge state, while the water level can be either improved or degraded depending on the coherence between the model and the observation H - Q relation.

The analyzed water level from ASSIM1 is then used as the background state for ASSIM2; it is compared to water level observations over the 6-hour assimilation period and the EKF update provides a correction to the river bed and flood plain friction coefficients m and n, which results in the water level improvement as shown in Figure 4 (squared solid line). The oscillations at the beginning of the cycle are due to the inconsistency between the initial state (stored from a previous cycle analysis) and the friction coefficients for the current cycle. The assimilation window is shifted hourly and the sequential application of ASSIM1+ASSIM2 provides a corrected hydraulic state and forecast. This cycled DA procedure allows for
a temporal variability of the friction coefficients over a flood event, which can be either
associated to real changes in the river bed and flood plain friction or geometry properties
as well as to various types of errors that are artificially accounted for here by correcting m and n.

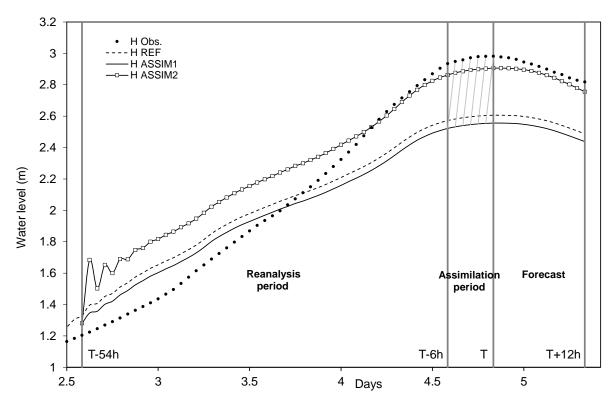


Figure 4: Observed (black dots), background from ASSIM1 (solid line) and analyzed (squared soline line) water levels for the ASSIM2 (following ASSIM1) approach at the flood peak at Mussey for the January 2004 flood event for T = 417,600 s = 4.83 days. Water level from ASSIM1 used as the background state for ASSIM2 is compared to water level observations to provide analyzed friction coefficients and subsequently, corrected water level.

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332 2.2.2. Study on the linear assumption of the generalized observation operator

The EKF algorithm relies on the hypothesis that the generalized observation operator can be approximated by a linear operator on the  $[\mathbf{x}^b, \mathbf{x}^a]$  interval. The linearity of the hydraulic model response to a perturbation in the river bed and flood plain friction coefficients mand n was thus investigated. Figure 5 presents the probability density function (pdf) of the simulated water level at Mussey for a permanent flow ( $Q = 150 \text{ m}^3/\text{s}$ ) when the friction coefficient at Mussey for the minor bed is perturbed around the background mean value m = 20. The 10,000 perturbations are randomly chosen following a Gaussian function with a variance of 12.

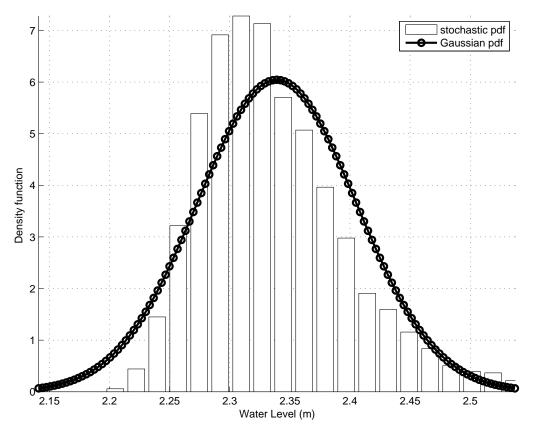


Figure 5: Water level pdf for 10,000 perturbations of the river bed friction coefficient m with a variance of 12. The solid line represents the analytical pdf corresponding to a Gaussian model response; and the histogram represents the actual MASCARET hydraulic model response reconstructed from the 10,000 model outputs.

In Figure 5, the pdf in solid line is a Gaussian function built from the first two moments 341 (mean and variance) of the system response assuming a linear relation in the model. The 342 actual response is represented by the shaded histogram that is obviously non-symmetrical. 343 First, there is a larger amount of water-level values that are smaller than the mean of the 344 Gaussian pdf. This means that the (negative) water level anomaly resulting from a small 345 positive perturbation  $\delta m$  of the friction coefficient is bigger than the (positive) water level 346 anomaly resulting from a negative perturbation  $-\delta m$  of the friction coefficient. Secondly, 347 the stochastic pdf is amplified for extreme water level values, meaning that a large (negative) 348 perturbation of the friction coefficient m results into a large (positive) perturbation of the 349 water level when a large (positive) perturbation of the friction coefficient has a smaller 350 impact. The same test was carried out with n; similar conclusions were drawn. It was also 351 found that the impact of a perturbation of m and n increases when the discharge increases. 352 Figure 6 assesses the impact of a perturbation  $\delta n$  (where  $x^{b} = 13$ ) between -12 and 12 on the 353 simulated water level at Mussey for different discharges. A perturbation of -6 for n leads to 354 a variation of 0.01 m when  $Q = 80 \text{ m}^3/\text{s}$  and to a variation of 0.03 m when  $Q = 225 \text{ m}^3/\text{s}$ . 355 Based on these results, it is assumed in the following that the relation between the friction 356 coefficients and the hydraulic state is reasonably approximated by a linear function in the 357 vicinity of  $\mathbf{x}^{\mathbf{b}}$ . The Jacobian matrix of the generalized observation operator  $\mathbf{H}_k$  is computed 358 around the background values for m and n for a perturbation  $\delta m = -2$  and  $\delta n = -1$  using 359 a finite differences scheme in consistency with the linearity study. In order to avoid non-360 physical values for the friction coefficients as well as to limit the nonlinear impact, minimum 361 and maximum threshold values are applied to the friction coefficients with [14, 24] for m 362

### 364 3. Correction of the model H - Q relation

and [8, 20] for n.

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#### 365 3.1. Bathymetric profiles densification (BATHY)

This section presents the method for experiment BATHY; it is assumed that the H - Qrelation in the 1D hydraulic model is improved by adding geometric data to the model.

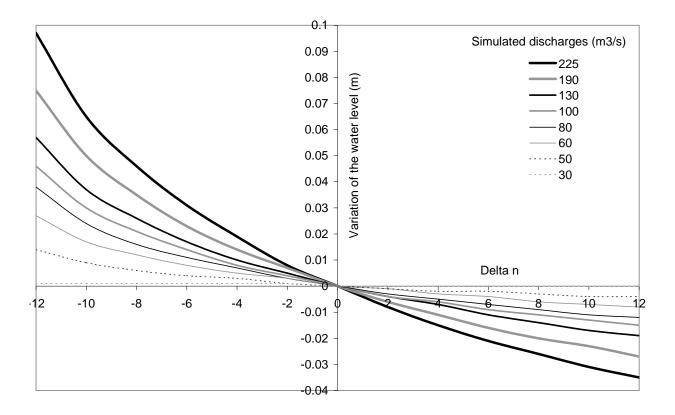


Figure 6: Impact of the flood plain friction coefficient perturbations  $\delta n$  on the water level [m] for different simulated discharges [m<sup>3</sup>/s]. A -10 and +10 perturbation of ngenerates a non equivalent variation of the water level but for low perturbations, the relation between friction coefficients and water level can be considered as linear.

Additional measurements of the river bed and flood plain geometry were made available near 368 Mussey: 4 topographic and bathymetric measurements were performed in the surrounding 369 of the observing station. The batch calibration of the local friction coefficients was then 370 re-processed on sections 1 and 2 for reach 4. The friction coefficients for these two sections 371 were set to m = 30 and n = 8. Figure 2 illustrates the positive impact of the cross-section 372 densification for the January 2004 flood event for water level (dashed line with triangles). As 373 presented in Table 2, for experiment BATHY, the Nash-Sutcliffe criterion for H is improved 374 from 0.773 to 0.923, even though a 10-cm underestimation remains. The discharge results 375 are left unchanged by this local bathymetry correction with a 0.897-Nash-Sutcliffe coefficient 376 for BATHY (compared to 0.894 for REF); a small overestimation at the flood peak remains 377

(10 m<sup>3</sup>/s) for this event. As shown in Table 3, the Nash-Sutcliffe criteria values computed
for water level over the eight validation flood events in re-analysis mode for BATHY are
better than those computed for REF, especially at Mussey where the additional geometry measurements were made; in contrast, the impact at Joinville is small.

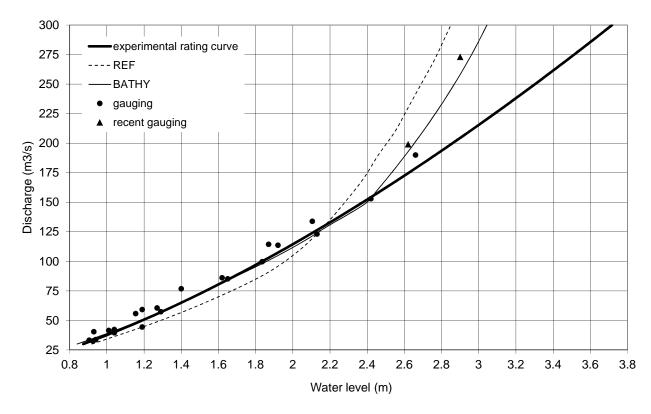


Figure 7: Comparison of the H - Q relation at Mussey, derived experimentally (thick solid line) from gauging (black dots/triangles), involved in the reference model REF (thin dashed line) and obtained through the BATHY approach (thin solid line). Recent gaugings are represented with black triangles.

381

In Figure 7 the H - Q relation for REF is represented by the thin dashed line, and the H - Q relation for BATHY is represented by a thin solid line. It is shown that the BATHY H - Q relation is in better agreement with all available gauging (black dots and triangles) than the REF H - Q relation. As a consequence, the new model H - Q relation should be used to produce discharge data from water level measurements at Mussey, in place of the experimental rating curve (thick solid line) that is in good agreement with low

Observing stations	Mu	Joinville	
Observing stations	$N_H$	$N_Q$	$N_H$
Forecast lead time	0h	0h	0h
REF	0.601	0.722	0.653
BATHY	0.681	0.721	0.661
ASSIM1	0.754	0.854	0.779
BATHY+ASSIM1	0.858	0.853	0.784
ASSIM1+ASSIM2	0.859	0.842	0.992
Forecast lead time	12h	12h	12h
REF	0.135	0.238	0.154
BATHY	0.272	0.241	0.158
ASSIM1	0.689	0.807	0.695
BATHY+ASSIM1	0.781	0.802	0.698
ASSIM1+ASSIM2	0.832	0.807	0.907

Table 3: Nash-Sutcliffe criteria for REF, BATHY, ASSIM1, ASSIM1+ASSIM2 and BATHY+ASSIM1 computed over eight flood events for 2004-2013 at maximum lead time (12 hours) at Mussey and Joinville.

flow measurements but can lead to an underestimation of up to 60  $m^3/s$  for high flow. It 388 should be noted that the experimental rating curve was built from numerous gaugings below 389 150  $\text{m}^3$ /s (black open dots) and only two gaugings above 150  $\text{m}^3$ /s. Additionally, two recent 390 gaugings for high flow (black triangles) allow to validate the BATHY model H - Q relation 39: over the entire range of discharge values at the observing station. Figure 2 presents the 392 corrected observed discharges that are derived from water level measurements at Mussey 393 using the BATHY densified model H - Q relation (black circles). Using these corrected 394 measurements, the model now slightly underestimates both water level (thin dashed line) 395 and discharge (thick dashed line) at the flood peak. The sign of the errors in discharge and 396 water level are now the same over the entire flood event, meaning that the optimization of 397 upstream and lateral inflows as proposed in (13) is an appropriate solution for further flood 398

<sup>399</sup> forecast improvement for both discharge and water level states.

#### 400 3.2. Data assimilation for friction coefficients correction (ASSIM)

In this section, it is assumed that no additional geometric measurement is available. The reference model H - Q relation is improved accounting for errors in friction coefficients and by artificially accounting for local bathymetry error with the sequential estimation of the river bed and flood plain friction coefficients m and n in the surrounding of the observing stations at Mussey and Joinville (experiment ASSIM).

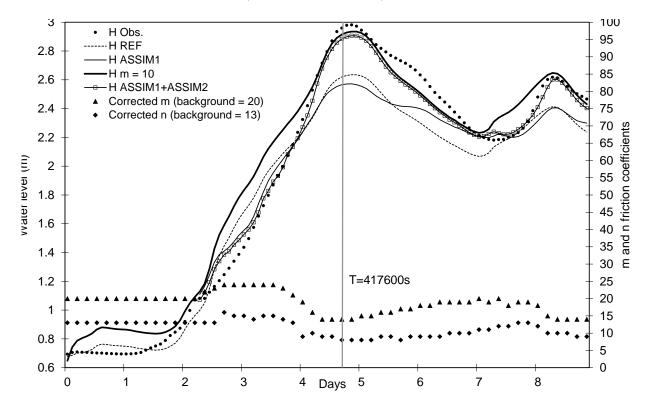


Figure 8: Observed water levels, REF (dashed line), model with m = 10 (thick solid line), background from ASSIM1 (thin solid line), ASSIM1+ASSIM2 (squared solid line) for the January 2004 flood event at Mussey. Corrected friction coefficients for river bed (m) and flood plain (n) from DA analysis are represented with triangles and diamonds respectively.

405

Figure 8 illustrates that the water level can be efficiently increased at Mussey, compared to that of REF (m = 20 and n = 13 represented with a thin dashed line), when decreasing the

river bed friction coefficient to m = 10 (thick solid line), while discharges are left unchanged 408 (not shown). The value m = 10 is appropriate for high flow but leads to a water level 409 overestimation for low flow condition. The friction coefficient estimation should then be flow 410 dependent and provide time-dependent friction coefficients that account for varying errors in 411 the friction and bathymetry river bed as the flow occupies a varying portion of the river and 412 the flood plain. For this purpose, the DA method ASSIM detailed in Sect. 2.2 is cycled over 413 the entire flood event to estimate upstream and lateral inflows (ASSIM1), and river and flood 414 plain friction coefficients (ASSIM2) over time using hourly observed discharge and water level 415 at Mussey. Corrected lateral and upstream forcings from ASSIM1 are used to provide the 416 background state (thin solid line) for the friction coefficient estimation in ASSIM2. It should 417 be noted that while ASSIM1 leads to a significant correction of discharge, the water level in 418 ASSIM1 remains close to that of REF. The ASSIM1+ASSIM2 DA analysis for water level is 419 presented for time T from day 2.25 to the end of the flood event in Figure 8 (squared line). 420 For instance, at day 3, REF overestimates the water level, ASSIM1+ASSIM2 increases the 421 friction coefficients in order to decrease the simulated water level. On the contrary, over 422 the flood peak period (days 4-7), REF underestimates the water level, ASSIM1+ASSIM2 423 decreases the friction coefficients in order to increase the simulated water level. 424

The Nash-Sutcliffe criteria for water level and discharge computed at Mussey for January 425 2004 in re-analysis mode are presented in Table 2. ASSIM1 improves the discharge Nash 426 value from 0.894 (REF) to 0.976; it is not significantly affected by ASSIM2 (0.978). The 427 water level Nash value is not significantly modified by ASSIM1 (0.773 for REF compared to 428 0.784 for ASSIM1); it should be noted that ASSIM1 can either lead to an improvement or 429 a degradation of the water level (as it is the case at the flood peak). However, it is greatly 430 improved with ASSIM2 to 0.97. These results are also obtained over the eight validation 431 flood events: the Nash-Sutcliffe criteria computed at Mussey and Joinville in re-analysis 432 mode (0-hour forecast lead time) as well as at the maximum lead time forecast (12 hours) 433 are presented in Table 3 for REF, BATHY and ASSIM. In re-analysis mode, ASSIM1 greatly 434 improves the discharge results, while ASSIM2 provides improved water level states at Mussey 435 and Joinville since the friction coefficients are corrected in the vicinity of both observing 436

stations. In forecast mode, the upstream and lateral hydrologic forcings are supposed to 437 be unknown and set constant to the last observed value. As a consequence, the Nash-438 Sutcliffe coefficients for REF and BATHY decrease as the forecast lead time increases. The 439 correction of upstream and lateral inflows from ASSIM1 enables a correction of the forcing 440 over the forecast period, thus allowing for a significant improvement of the results at a 12-44: hour forecast lead time. The water level Nash criteria is further improved by ASSIM2 for 442 Mussey and Joinville. For ASSIM1 and ASSIM2, it is assumed that the correction computed 443 over the analysis period can be applied over the forecast period; as the nature of the errors 444 varies in time, this assumption is less and less valid as the forecast lead time increases and 445 the merits of ASSIM decrease. 446

It should be noted that the local densification of the geometric description (BATHY) 447 when applied sequentially with ASSIM1, leads to similar results to ASSIM1+ASSIM2 at 448 Mussey but not at Joinville, where no additional bathymetric measurements were available. 449 ASSIM thus appears as an efficient approach for improving and forecasting both discharge 450 and water level given no additional data on the river bed and flood plain geometry. Fol-45 lowing these tests, the approach ASSIM1+ASSIM2 has become recently operational at SPC 452 SAMA: the assimilation of discharge measurements used in real-time mode to better quan-453 tify upstream and lateral inflows (ASSIM1) has successfully run since December 2013; the 454 extension of the control vector to the river bed and flood plain friction coefficients (ASSIM2) 455 has recently been added into the operational flood forecasting chain and has shown very good 456 results. The details for the ASSIM implementation in the framework of operational flood 457 forecasting are given in Sect. 4. 458

#### 459 4. Operational implementation at SPC SAMA

The SPC SAMA transfers a vigilance map to SCHAPI twice a day at 8:45 a.m and 2:45 p.m so that the national vigilance map can be issued at 10:00 a.m and 4:00 p.m. The realtime forecast operational chain for the Marne Amont Global (MAG) hydraulic model using DA from the ASSIM1+ASSIM2 previsouly described approach is presented in Figure 9 and

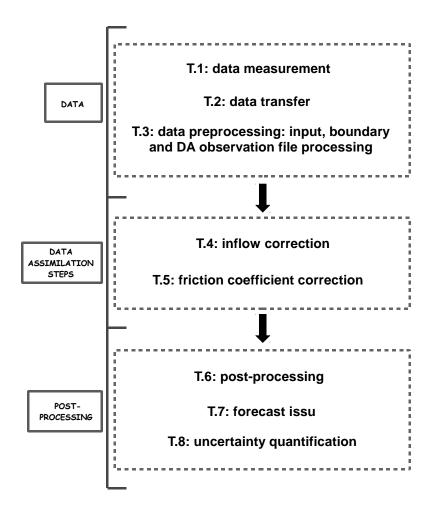


Figure 9: Operational organigram for DA applied to the Marne Amont forecast model divided in eight tasks.

is broken down in three modules. This chain should be computationally efficient to allowfor the use of recently acquired data while providing informed forecasts.

The first module, named DATA, is composed of three tasks. In task 1, in-situ measurement of water levels are made at approximately 50 observing stations with automatic instruments over the SAMA catchment. In task 2, these data are gathered at SPC through telephone network four times a day, up to hourly during a flood event. The quality of these data is controlled and, when not observed, discharge data are computed using a local rating curve. Task 3 consists in pre-processing the observed data to provide to input files for the hydraulic model. Depending on the average flow conditions in the network, an initialisation file for the MAG model is chosen amongst a pre-computed input files data base for low, medium and high flow. Using data from the upstream observing stations, 9 files for the boundary conditions for the hydraulic network are automatically generated for each analysis time T over [T-54h,T], with a constant extension over [T,T+21h] (maximum lead time at Chamouilley). Water level and discharge observations files are automatically generated at the assimilation station of Condes, Mussey, Joinville, Chamouilley and Saucourt over [T-6h,T] for the assimilation analysis.

The second module, DA STEPS, gathers two tasks that launch the DA steps. Task 4 480 represents the ASSIM1 step of the DA procedure : observed discharges are assimilated at 48 Condes, Mussey, Chamouilley and Saucourt to correct upstream and lateral inflows. The 482 corrected forcing files are stored for use in task 5. Task 5 represents the ASSIM2 step of the 483 DA procedure: observed water levels at Joinville are assimilated to correct the local friction 484 coefficients. The improved bathymetry from BATHY in the neighboring of Mussey is used 485 in the operational model MAG, thus improving the model H - Q relation locally. As a 486 consequence, there is no need to assimilate observed water level at Mussev. 487

The third module is dedicated to POST-PROCESSING of the analysis. The REF and ASSM1+ASSIM2 result files are exported in task 6 to a server for post-treatement using a supervision software that provides the forecaster with an integrated hydrological situation of the catchment. In task 7, based on the provided forecast and his expertise, the forecaster is finally able to characterize the flood risk within the risk-color panel.

In the third module, this information is then published by SCHAPI on the vigicrues 493 web site and communicated to the Civil Services. Task 8 is dedicated to quantifying the 494 uncertainty (UQ) related to the forecasted water level. Considering a gaussian-shaped error 495 on the controled friction coefficients and forcing corrective parameters, the analysis error 496 is used to define a so-called analysis interval between the 10th and the 90th quantiles. 497 Integrating a limited number of additional model runs for these interval limits thus provides 498 an on-line envelope for forecasted water level. An additional information on the forecasted 499 water level is given by a set of abacus that are set up off line. The difference between the 500 simulated and observed water level for the eight validation flood events are computed and 501

classified in quantiles for each forecast lead time. The median, 10th and 90th quantiles are 502 identified and used in the operational chain to provide an uncertainty range for the analysed 503 water level. The computational cost of the full chain is about 4 minutes on a mono processor 504 work station. Both uncertainty ranges are represented in Figure 10 for the Decembre 2011 505 event at Joinville. On December 18th at 1 p.m, the REF model (dashed line) overestimates 506 the observed water level (black dots) reaching the orange threshold. ASSIM1+ASSIM2 507 analysis (squared solid line) provides a water level that is below the threshold with an 508 uncertainty range that remains below (or extremely close to) the orange threshold for both 509 off-line and on-line UQ methods (grey and hatched envelopes). 510

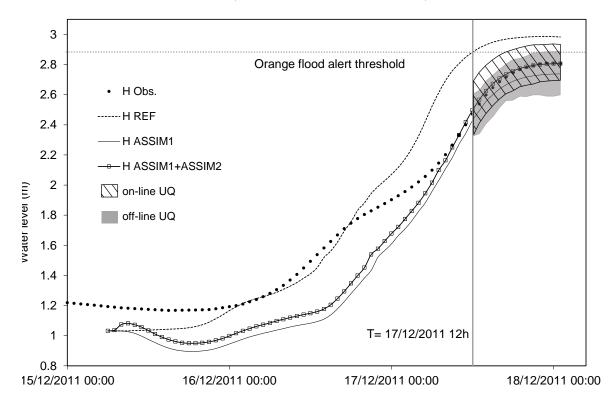


Figure 10: Observed water level (black dots) and forecasts for REF (dashed line), background from ASSIM1 (thin solid line) and ASSIM1+ASSIM2 (squared solid line) at Joinville for the December 2011 flood event. Uncertainties computed with on-line and off-line methods are represented with grey-colored and hatched areas.

#### 511 5. Conclusion

This paper addressed the errors in the water level-discharge relation of a 1D hydraulic 512 model (MASCARET) in order to improve the forecasted water level state in the context of 513 operational flood forecasting; this water level is used to generate a colored flood risk map 514 at the French national level by SCHAPI. This improvement is obtained over the Marne 515 catchment through the integration of additional bathymetry data and water level measure-516 ments. In this work, it was first exhibited that a local densification of the description of the 517 river bed geometry leads to an improved water level simulation compared to the reference 518 model issued from a batch calibration process. The corrected bathymetry is used in the 519 model to build a rating curve that is found to be in good agreement with recent high flow 520 gauging. In operational context, this new rating curve is used to provide discharge from 521 hourly observed water level. At high flow, both water level and discharge are slightly under-522 estimated. The model can thus be improved by sequentially correcting the upstream and 523 lateral inputs to the models that are known to be imperfect approximation of hydrologic 524 flows for the hydraulic network. In an alternative strategy, it was assumed that no addi-525 tional bathymetry measurement could be made and that the water level-discharge relation 526 was improved by sequentially correcting the river bed and flood plain friction coefficients. 527 An extended Kalman filter (EKF) algorithm assimilates first hourly discharge observations 528 to correct inflows, then water level observations are assimilated to locally correct the friction 529 coefficients. This sequential approach provides a time-dependent correction of the friction 530 coefficients that accounts for errors in the friction and bathymetry description that vary 531 along with the flow as water level reaches different portions of the described geometry. A 532 sensitivity study showed that the model response is weakly nonlinear with respect to the 533 friction coefficients when the perturbation in the friction coefficient values remains bounded. 534 Both methods were applied in operational context and the Nash-Sutcliffe coefficient for both 535 water level and discharge was computed over eight validation flood events and greatly im-536 proved compared to the reference model. 537

At SPC SAMA, both approaches are currently used for operational flood forecasting. The

densified bathymetry description is used in the neighboring of the Mussey observing station 539 and water level data are assimilated to improve the water level-discharge relation in the 540 model in the neighboring of the Joinville observing station. An estimation of the analyzed 541 water level is also provided based on off-line abacus computed from a set of comparisons 542 between the model and the observations over past events. The two-step EKF-based data 543 assimilation approach also provides an error analysis variance for the river bed and flood 544 plain friction coefficients that are used to describe a confidence interval for the forecasted 545 water level. 546

In further work, the control vector should be extended to bathymetry profiles using 547 parametric correction, in order to limit the equifinality issue as well as the size of the control 548 vector to remain compatible with operational framework. The friction coefficients correction 549 will be extended to long-distance reaches; it should allow for a temporal adjustment over a 550 flood event and thereby for a significant improvement of the forecast lead time. A spatially 551 and time varying correction of the hydraulic parameters is the next challenge in line. For 552 that purpose, the use of spatially distributed data such as remote sensing data should be 553 investigated. High-resolution data with global coverage such as those from the upcoming 554 SWOT (Surface Water and Ocean Topography) mission will provide a new way to fully 555 describe the river hydrodynamics. Operational flood forecasting centers should thus be 556 prepared to make the most of the combination of remote sensing and in-situ data to design 557 future vigilance products. 558

#### 559 Acknowledgment

The financial support provided by SCHAPI, DREAL and SPC SAMA was greatly appreciated. The authors also gratefully acknowledge Florent Duchaine, Thierry Morel, Anthony Thévenin (CERFACS) for support on OpenPALM and on the Parasol functionality.

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This paper presents a data-driven hydrodynamic simulator based on the 1-D hydraulic solver dedicated to flood forecasting with lead time of an hour up to 24 hours. The goal of the study is to reduce uncertainties in the hydraulic model and thus provide more reliable simulation and forecast in real time for operational use by the national hydrometeorological flood forecasting center in France. Previous studies have shown that sequential assimilation of water level or discharge data allows to adjust the inflows to the hydraulic network resulting in a significant improvement of the discharge while leaving the water level state imperfect. Two strategies are proposed here to improve the water level-discharge relation in the model. At first, a modeling strategy consists in improving the description of the river bed geometry using topographic and bathymetric measurements. Secondly, an inverse modeling strategy proposes to locally correct friction coefficients in the river bed and the flood plain through the assimilation of in-situ water level measurements. This approach is based on an Extended Kalman filter algorithm that sequentially assimilates data to infer the upstream and lateral inflows at first and then the friction coefficients. It provides a time varying correction of the hydrological boundary conditions and hydraulic parameters.

The merits of both strategies are demonstrated on the Marne catchment in France for eight validation flood events and the January 2004 flood event is used as an illustrative example throughout the paper. The Nash-Sutcliffe criterion for water level is improved from 0.135 to 0.832 for a 12-hour forecast lead time with the data assimilation strategy. These developments have been implemented at the SAMA SPC (local flood forecasting service in the Haute-Marne French department) and used for operational forecast since 2013. They were shown to provide an efficient tool for evaluating flood risk and to improve the flood early warning system. Complementary with the deterministic forecast of the hydraulic state, an estimation of an uncertainty range is given relying on off-line and on-line diagnosis. The possibilities to further extend the control vector while limiting the computational cost and equifinality problem are finally discussed.